

## Slovníky: Zhrnutie

| Metóda  | Insert  | Search   | Delete  | Analýza  |
|---|---|--|---|--|
| Spájaný zoznam                                    | $\Theta(1)$   | $\Theta(n)$  | $\Theta(n)$   | worst-case                                       |
| Utriedené pole                                    | $\Theta(n)$   | $\Theta(\log n)$   | $\Theta(n)$   | worst-case                                       |
| Hašovanie s reťazením<br>— s otvorenou adresáciou | $\Theta(1)$<br>$\Theta(1)$<br>$\Theta(n)$<br>$\Theta(\frac{1}{1-\alpha})$ | $\Theta(n)$<br>$\Theta(1 + \alpha)$<br>$\Theta(n)$<br>$\Theta(\frac{1}{\alpha} \ln \frac{1}{1-\alpha})$<br>or $\Theta(\frac{1}{1-\alpha})$ | $\Theta(n)$<br>$\Theta(1 + \alpha)$<br>$N/A$<br>$N/A$ | worst-case<br>expected<br>worst-case<br>expected |
| Binárne vyhľ. stromy                              | $\Theta(n)$   | $\Theta(n)$  | $\Theta(n)$   | worst-case                                       |
| AVL stromy  | $\Theta(\log n)$  | $\Theta(\log n)$   | $\Theta(\log n)$                                      | average  |
| Scapegoat stromy                                  | $\Theta(\log n)$  | $\Theta(\log n)$   | $\Theta(\log n)$                                      | worst-case                                       |
| Tries (string of length $m$ )                     | $\Theta(m)$   | $\Theta(m)$  | $\Theta(m)$   | amortized  |
|   |   |  |   | worst-case                                       |

```
Rabin-Karp(T[1..n],P[1,,m]):  
    hashp = hash(P,1)  
    hasht = hash(T,1)  
  
    for i:=0 to m-n  
        // inv: hasht = hash(T,i+1)  
        if (hashp = hasht)  
            // check whether T[i+1..i+m] matches the pattern  
            valid = true  
            for j = 1 to m  
                if P[j] != T[i+j]  
                    valid = false; break loop  
                if valid then output i  
    hasht = shift_hash(T,i+1,hasht)
```

- veľkosť abecedy:  $k$
- hašovacia funkcia:  $(S[i]S[i+1]\dots S[i+m-1]) \text{ mod } q$
- predpočítaná hodnota:  $ktmm1 = k^{m-1} \text{ mod } q$

`hash(S, i):`

```
// compute hash of S[i]S[i+1]...S[i+m-1]
result = 0
for j = 0 to m-1
    result = (10*result + S[i+j]) mod q
return result
```

`shift_hash(S, i, oldhash):`

```
// compute hash of S[i+1]S[i+2]...S[i+m]
// given that oldhash is a hash of S[i]S[i+1]...S[i+m-1]
return ((oldhash + q - (S[i]*ktmm1 mod q))
        * k + S[i+m]) mod q
```

|    | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 |
|----|---|---|---|---|---|---|---|---|---|---|----|----|
| T: | b | a | n | a | n | a | n | o | b | a | n  | o  |

i=0: X

i=1: X

i=2: n a n X

i=3: X

i=4: n a n o

i=5: X

i=6: n X

i=7: X

i=8: X

i=9: n X

i=10: X

```
DFA_STRING_MATCHING(T[1..n],tr):  
    state:=0;  
    for i:=1 to n  
        state:=tr[state,T[i]]  
        if (state = m)  
            output shift i-m
```

```
CONSTRUCT_TRANSITION_FUNCTION(P[1..m]):  
    for i:=1 to m  
        for all characters c in alphabet Sigma  
            suffix := P[1..i].c  
            drop := 0  
            while suffix is not prefix of P  
                drop first character of suffix  
                drop := drop + 1  
            tr[i,c] := i+1-drop
```

```
KMP_STRING_MATCHING(T[1..n],pi):
    // P[m+1] = some character outside alphabet
    state := 0
    for i := 1 to n
        while state>0 and T[i]<>P[state+1]
            state := pi[state]
        if T[i] = P[state+1]
            state := state + 1
        if state = m
            output shift i-m
```

CONSTRUCT\_PREFIX\_FUNCTION( $P[1..m]$ ) :

```
pi[0]:=0;  
for i:=1 to m  
  q:=i-1; pi[i]:=0  
  while q > 0  
    q:=pi[q]  
    if P[q+1]=P[i] then  
      pi[i]:=q+1;  
      break loop;
```

```
CONSTRUCT_PREFIX_FUNCTION(P[1..m]):  
    pi[0]:=0;  
    q:=0;  
    for i:=1 to m  
        while q > 0 and P[q+1]<>P[i]  
            q := pi[q];  
        if pi[q+1] = pi[i]  
            q := q+1  
        pi[i] := q
```

## Vyhľadávanie v teste: Zhrnutie

| Algoritmus         | Predpočítanie | Vyhľadávanie              |            |
|--------------------|---------------|---------------------------|------------|
| Naivný algoritmus  |               | $O(mn)$                   | worst-case |
| Rabin-Karp         |               | $O(m + n + \frac{mn}{q})$ | expected   |
| Konečný automat    | $O(m^3)$      | $O(n)$                    | worst-case |
| Knuth-Morris-Pratt | $O(m)$        | $O(n)$                    | worst-case |
| Sufixový strom     | $O(n)$        | $O(m)$                    | worst-case |