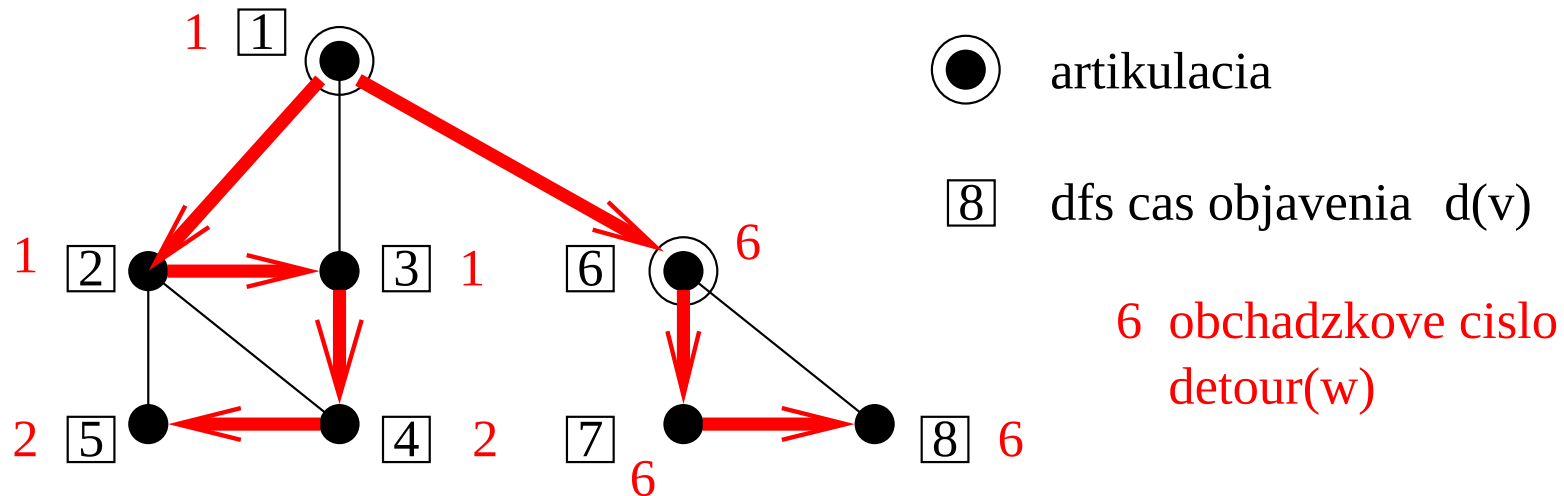




Def: Obchádzkové číslo vrchola v je najmenšie DFS číslo $d(w)$ vrchola w , ktorý môžeme dosiahnuť z vrchola v tak, že najskôr prejdeme niekoľko stromových hrán a potom jednu spätnú hranu.

Lema: Koreň DFS stromu je artikulácia práve vtedy, keď má v DFS strome viac ako jedno dieťa.

Lema: Vrchol v , ktorý nie je koreňom DFS stromu, je artikulácia práve vtedy, keď aspoň pre jedno jeho dieťa w v DFS strome platí $\text{detour}(w) \geq d(v)$.

Artikulácie: modifikácia prehľadávanie do hĺbky (vrchol, ktorý nie je koreň)

```
function dfs-visit(v,cnum)
    status[v]:=gray;
    time:=time+1; d[v]:=time;
*   detour[v]:=v;
    for each w in out(v)
        if status[w]=white
            //--- (v,w) is a TREE edge
            dfs-visit(w,cnum); // detour[w] is now computed!
*       if detour[w]>=d[v] then vertex v is an articulation!
*       if detour[w]<detour[v] then detour[v]:=detour[w];
*   else
*       //--- (v,w) is a BACK edge
*       if d[w]<detour[v] then detour[v]:=d[w];
    status[v]:=black;
```

Prehľadávanie do šírky (BFS)

```
function bfs-visit(v,cnum)
    create empty queue Q;
    status[v]:=gray;
    dist[v]:=0;
    enqueue(Q,v);

    while Q is not empty
        u:=dequeue(Q);
        num[u]:=cnum;
        for each w in out(u)
            if status[w]=white then
                status[w]:=gray;
                dist[w]:=dist[u]+1;
                enqueue(Q,w);
        status[u]:=black;
```

Dijkstrov algoritmus

```
// initialize dist, S, T
S:=0; T:=V;
for all w in V do dist[w]:=infinity;
dist[u]:=0;

// add one vertex at a time to T
while T is non-empty do
**s:=vertex for which dist[s] represent the length
**  of the shortest path from u to s;
  add s to S; remove s from T;
  // update dist to account for enlarged set S
  for all t in out(s) do
    // try to shorten current path to t through s
    if (dist[s]+w[s,t]<dist[t]) then
      dist[t]:=dist[s]+w[s,t];
```

Dijkstrov algoritmus

```
// initialize dist, S, T
S:=0; T:=V;
for all w in V do dist[w]:=infinity;
dist[u]:=0;

// add one vertex at a time to T
while T is non-empty do
    s:=vertex with the smallest dist[s];
    add s to S; remove s from T;
    // update dist to account for enlarged set S
    for all t in out(s) do
        // try to shorten current path to t through s
        if (dist[s]+w[s,t]<dist[t]) then
            dist[t]:=dist[s]+w[s,t];
```

Dijkstrov algoritmus (s rekonštrukciou ciest)

```
// initialize dist, S, T
S:=0; T:=V;
for all w in V do
* dist[w]:=infinity; last[w]:=undefined;
dist[u]:=0;

// add one vertex at a time to T
while T is non-empty do
    s:=vertex with the smallest dist[s];
    add s to S; remove s from T;
    // update dist to account for enlarged set S
    for all t in out(s) do
        // try to shorten current path to t through s
        if (dist[s]+w[s,t]<dist[t]) then
*         dist[t]:=dist[s]+w[s,t]; last[t]:=s;
```

```
// path reconstruction from u to v
w:=v; create an empty path;
while last[w]<>undefined do
    add w to the beginning of the path;
    w:=last[w];
```

Kruskalov algoritmus (minimálna kostra)

Sort edges in order of increasing weight

so that $w[f[1]] \leq w[f[2]] \leq \dots \leq w[f[m]]$

$T = \text{empty set}$

for $i := 1$ to m do

 let u, v be the endpoints of edge $f[i]$

 if there is no path between u and v in T then (**)

 add $f[i]$ to T

return T

