

# Final exam

- Do not forget to hand in your projects by **January 15 or 2 days** before the final exam, whichever comes first.
- You can bring a cheat sheet (2 sheets of A4, both sides)  
+ theoretical computer science cheat sheet
- **Written final exam:** model exam will be available next week  
40% of you total grade, you need to get at least 50% of points on the exam  
regular exam dates: 16.1.2020 (Thursday) 9:00-12:00  
22.1.2020(Wednesday) 9:00-12:00  
**sign up in AIS2 latest 2 days before the exam**
- Dates for repeat exams will be scheduled as needed.
- **To finalize your grade, we may ask you to come in to discuss and demonstrate your project.**

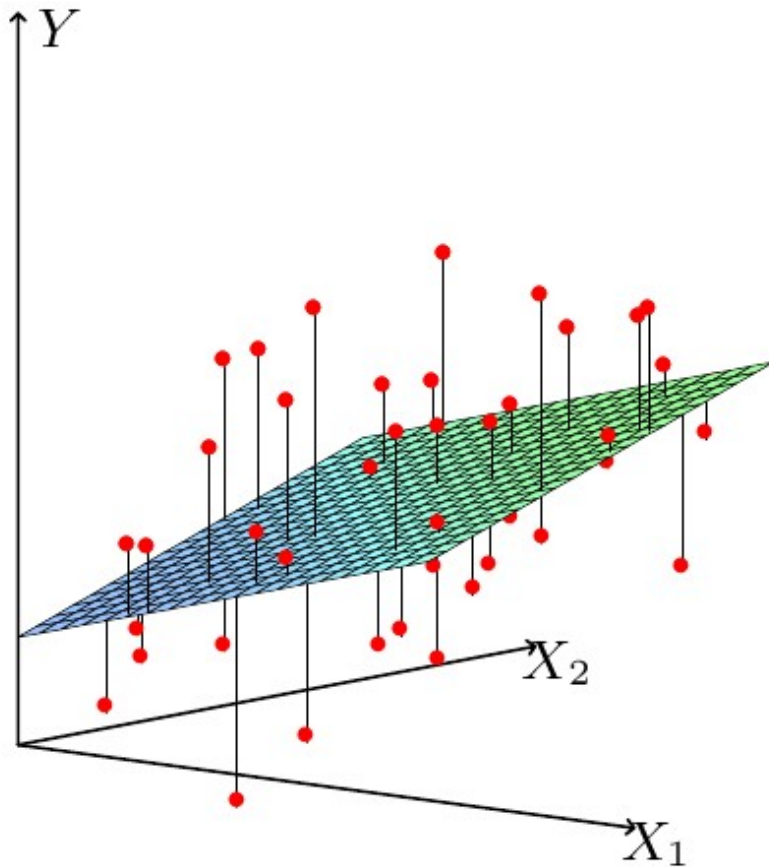


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**120%!**  
anketa  
[.fmph.uniba.sk](https://fmph.uniba.sk)

# Course Summary

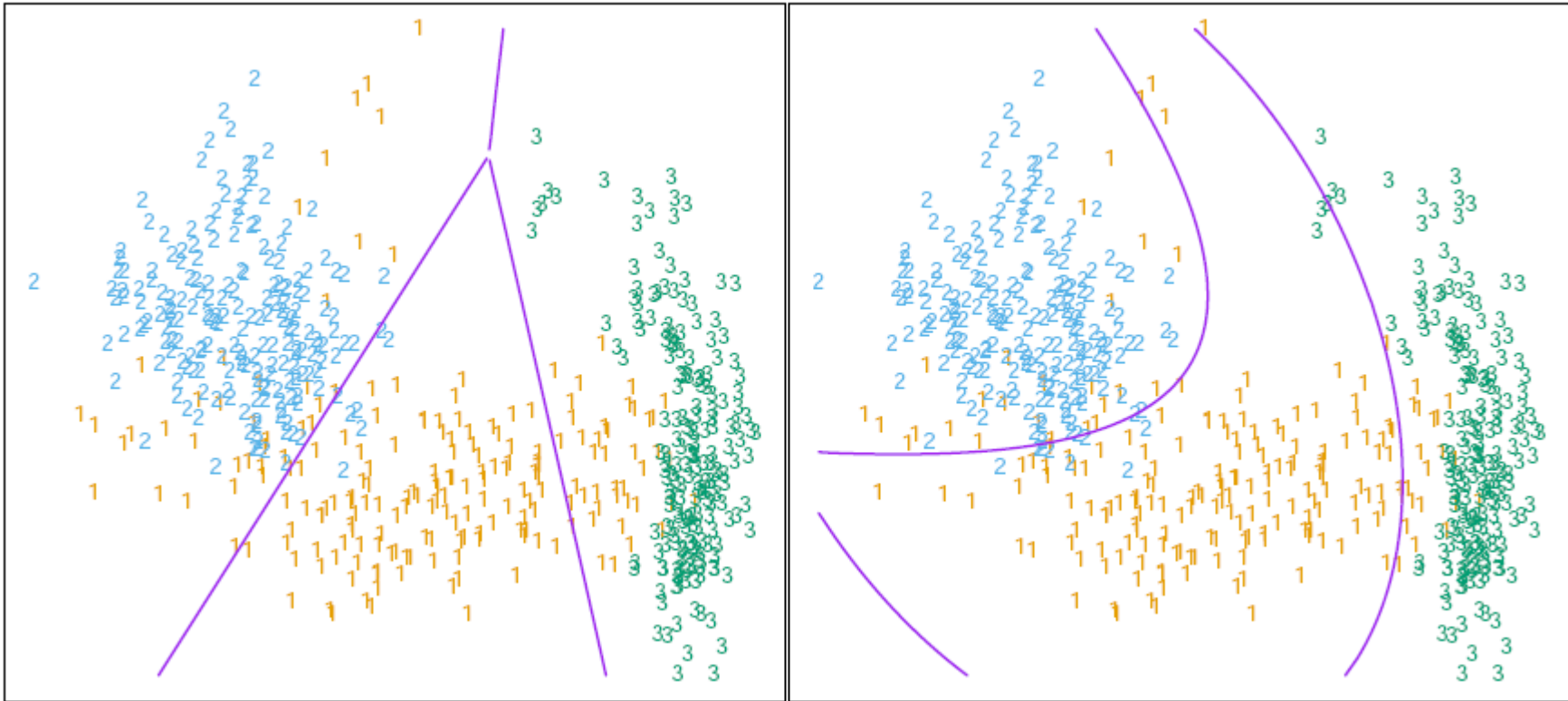
- **Supervised learning**
  - regression, classification
- **Unsupervised learning**
  - clustering, dimensionality reduction
- **Machine learning theory**
  - bias and variance, PAC learning, VC dimension
- **On-line learning and reinforcement learning**

# Regression



- Linear regression
- Solving normal equations in  $O(n^3)$
- Gradient descent
- Expansion of underlying vector space through non-linear transformation => generalized linear regression

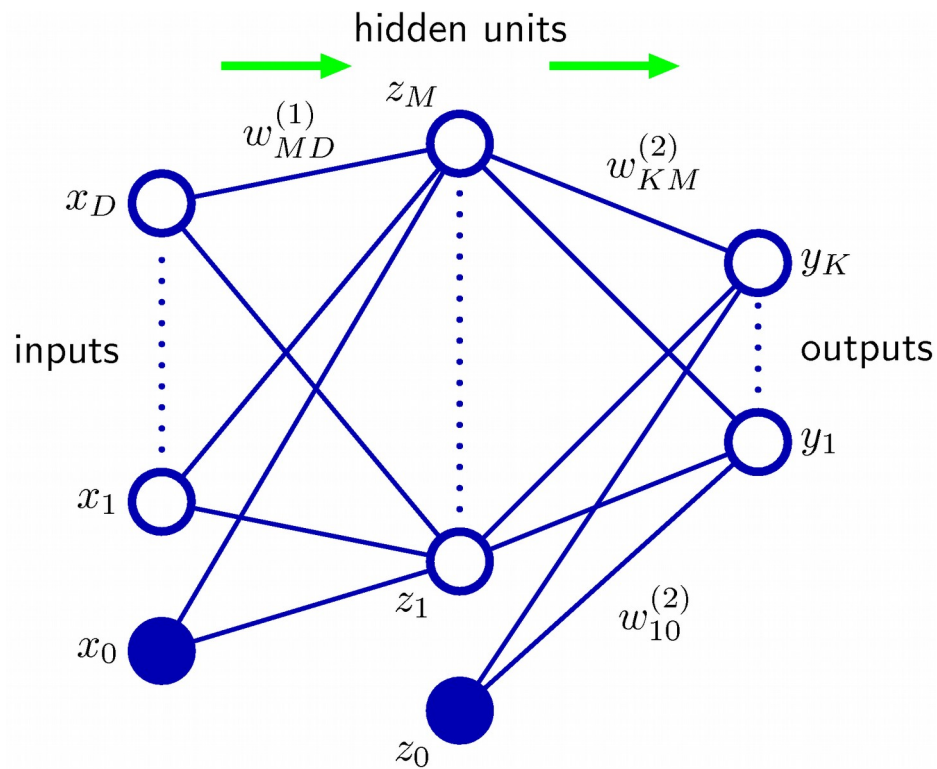
# Classification



Linear classification

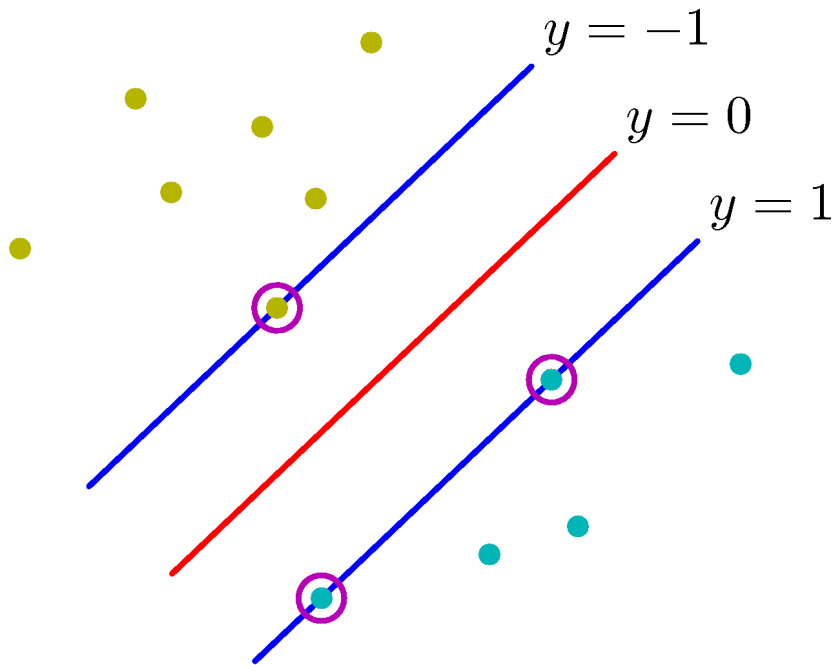
Using non-linear expansions

# Neural Networks



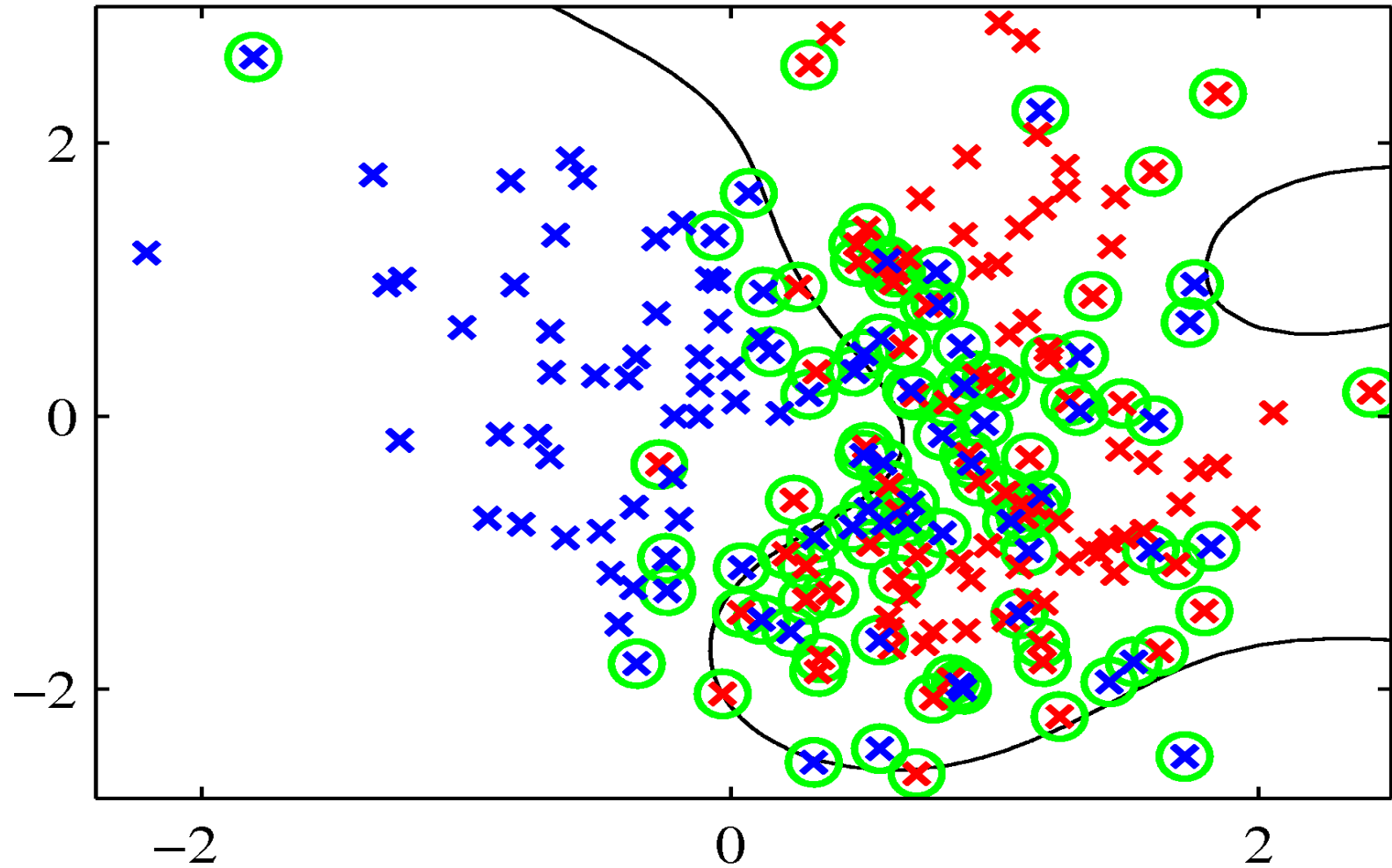
- Each unit (“neuron”) - linear combination followed by non-linear transformation
- Gradient descent (so called “back propagation”)

# Support Vector Machines



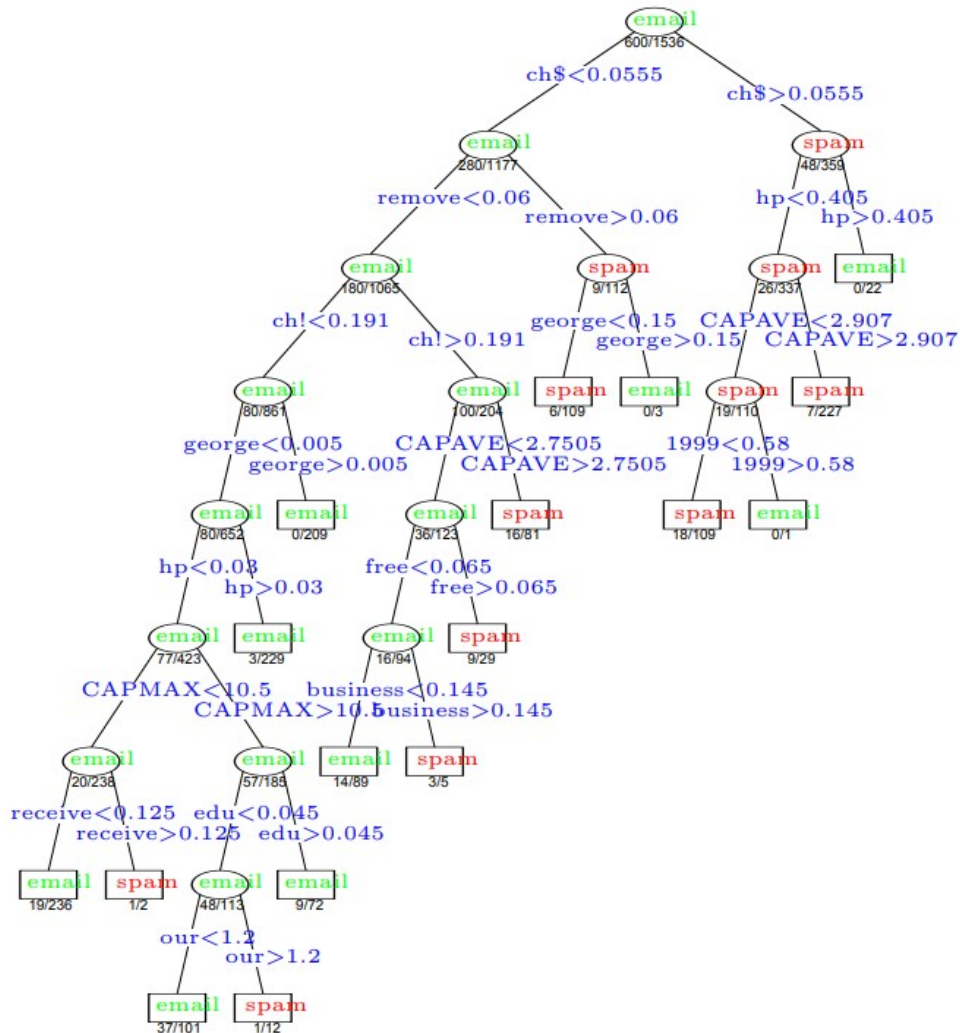
- Linear classifier maximizing margin
- Quadratic programming, dual programs
- Kernel trick:  
expansion into infinite dimensional vector space  
 $K(x,y)$  – dot product in the expanded space  
(intuition: similarity measure)

# Support Vector Machines



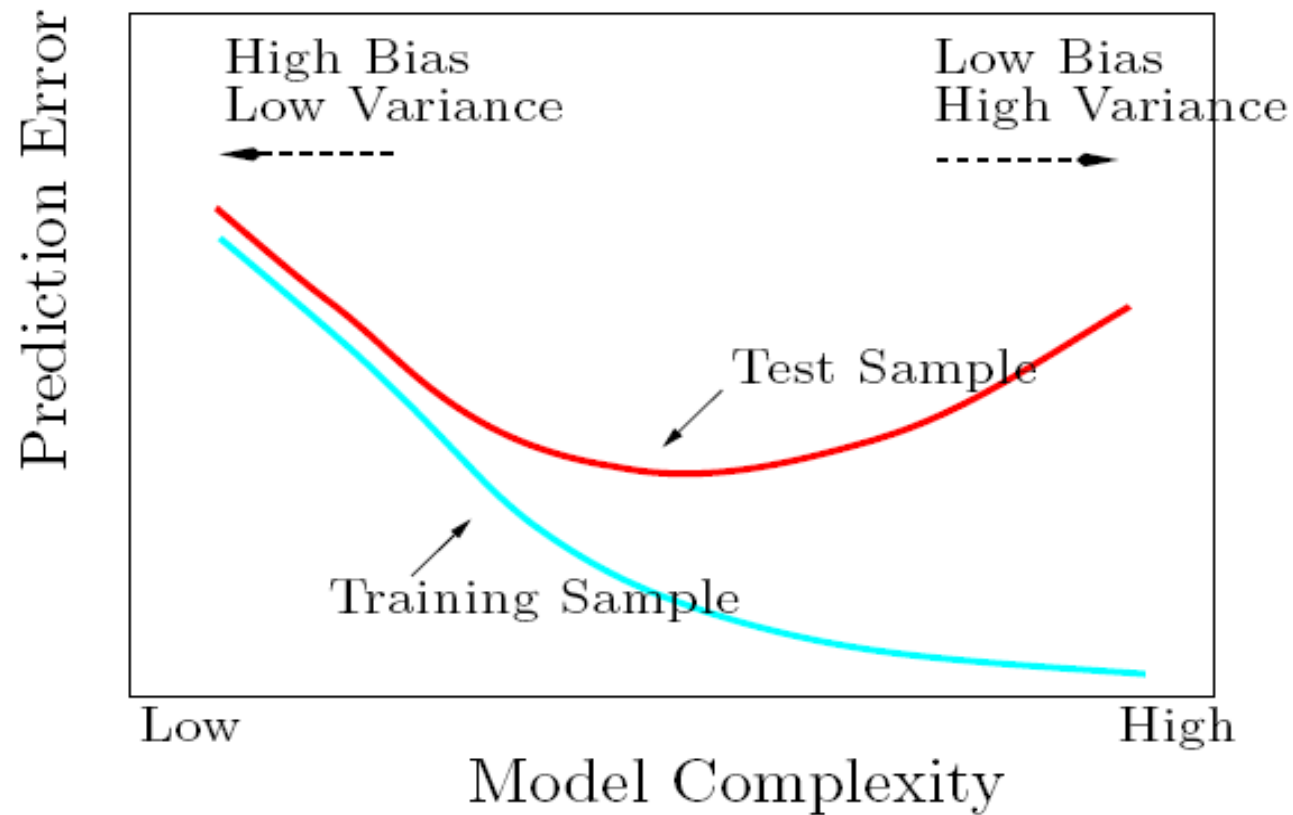


# Decision Trees and Random Forests



- ID3 algorithm for building trees (based on entropy measure)
- Stopping criteria
- Bagging – ensemble of complex classifiers
- Boosting – ensemble of simple classifiers

# Bias and Variance



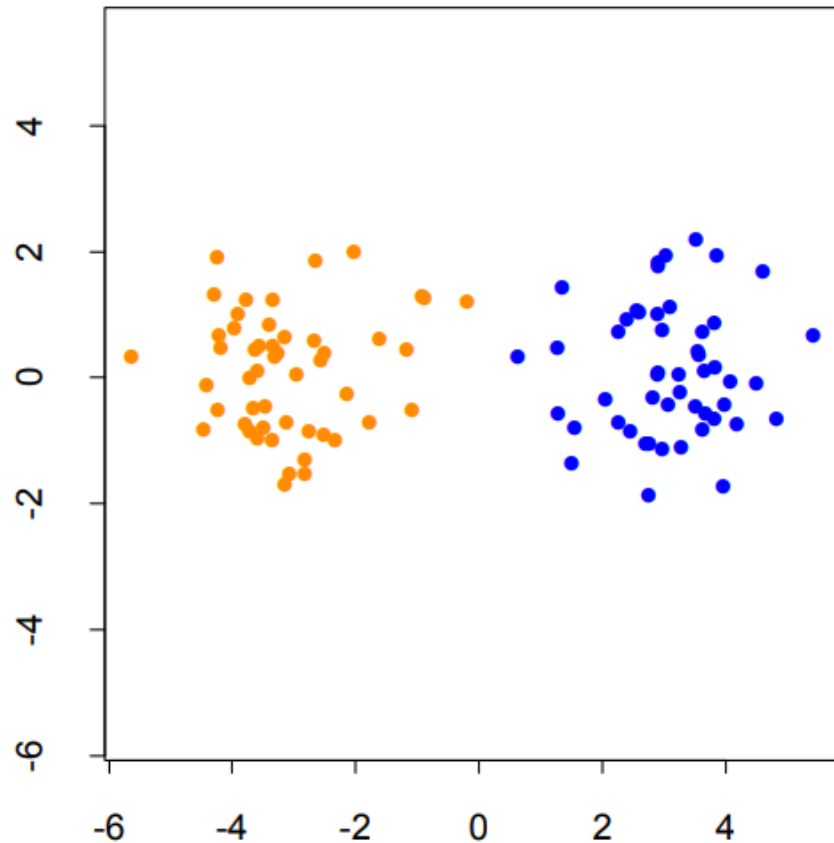
# PAC Learning (Probably Approximately Correct)

- How many training data points do we need to train a classifier?
- For large enough  $t$ ,  
**training and testing error  
with high probability ( $>1-\delta$ )  
will not differ much ( $<\epsilon$ )**
- PAC learning theory provides bounds on  $t$  for specific  $H$ ,  $\epsilon$  and  $\delta$

# PAC learning - bounds

- **Finite hypothesis space:**  
 $t = O(\log |H|)$
- **Infinite hypothesis space:**
  - Vapnik-Červonenkis (VC) dimension  $d$   
( $t$  grow linearly with  $d$ )  
Neural networks:  $d = \Theta(W \cdot \log n)$   
( $W$  – # weights,  $n$  – # sigmoids )
  - SVM:  $t = O(1/r^2 \log^2 1/r)$   
( $r$  – margin size)

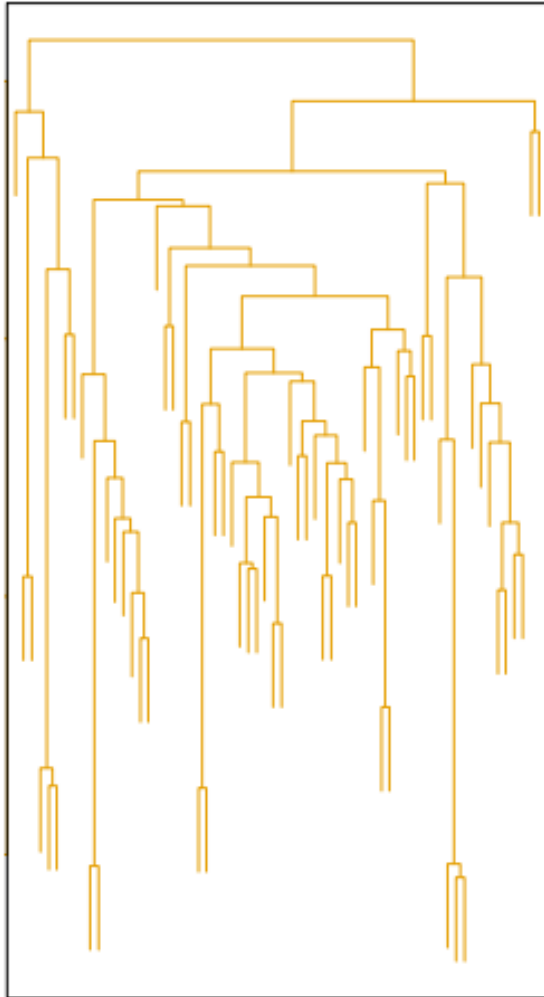
# Clustering



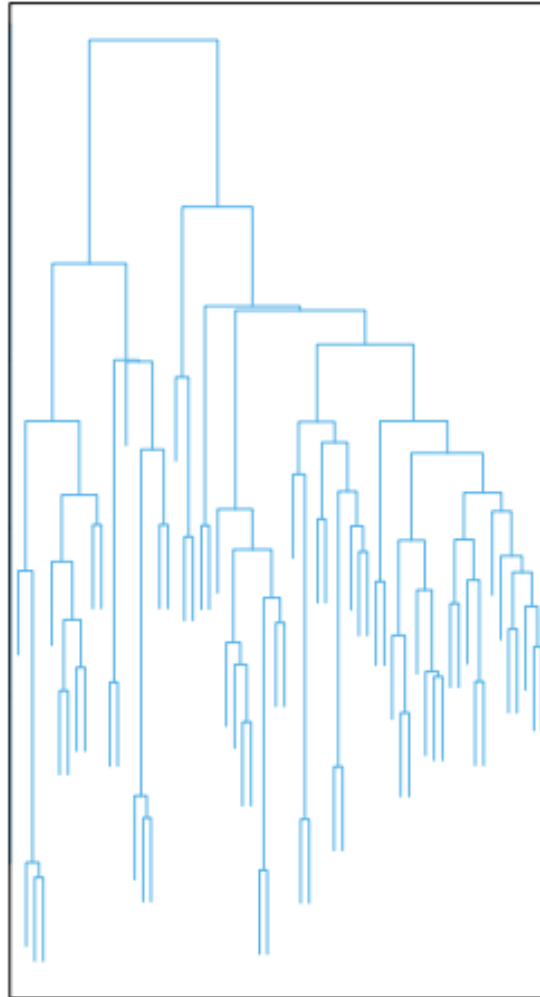
- K-means and k-medoids clustering
- Iterative methods to find a good solution
- Beware: slow!

# Hierarchical clustering

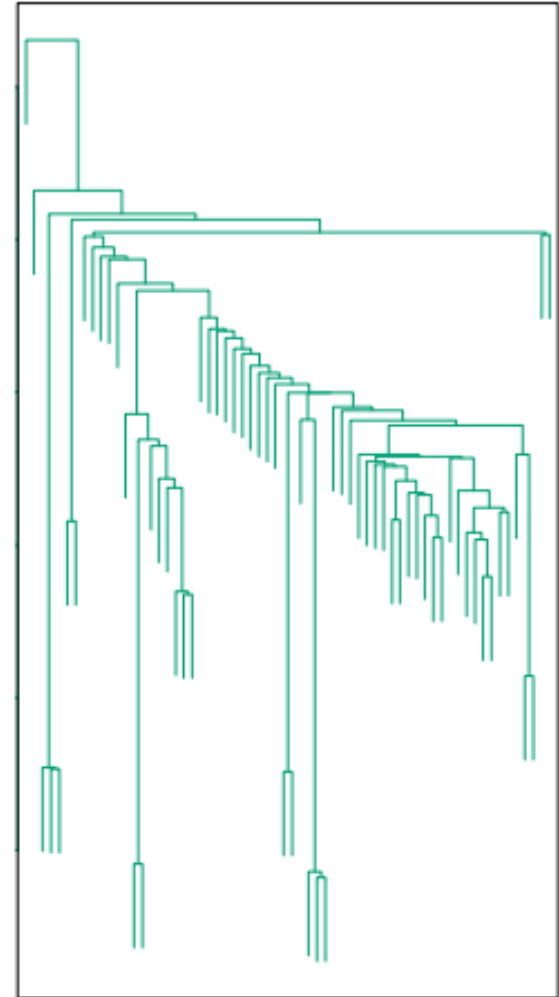
Average Linkage



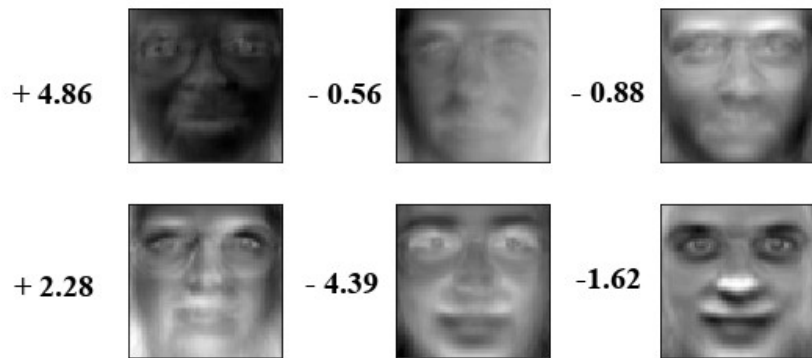
Complete Linkage



Single Linkage



# Dimensionality reduction



- Principal Component Analysis (PCA)
- Kernel trick (again)
- Multi-dimensional scaling (i.e. t-SNE)

# Mathematical Methods

- Matrix algebra, solving systems of linear equations
- Eigenvectors and eigenvalues
- Partial derivatives, Lagrange multipliers
- Numeral mathematics: Gradient descent
- Optimization: linear and quadratic programming, duality
- Analytical geometry
- Vector spaces



# (Un)related Classes

## **Spring 2020:**

- 2-INF-188: Current Topics in Machine Learning (Boža)
- 2-AIN-132: Neural Networks (Farkaš)
- 2-AIN-235: AI Algorithms in Robotics (Petrovič)
- (2021) 2-AIN-288: Speech Recognition

## **Fall 2020:**

- 1-BIN-301: Methods in Bioinformatics (Vinař, Brejová)
- 2-AIN-268: Deep Learning in Computer Vision (Černeková)
- 2-PMS-129: Stochastic Optimization Methods (Harman)