

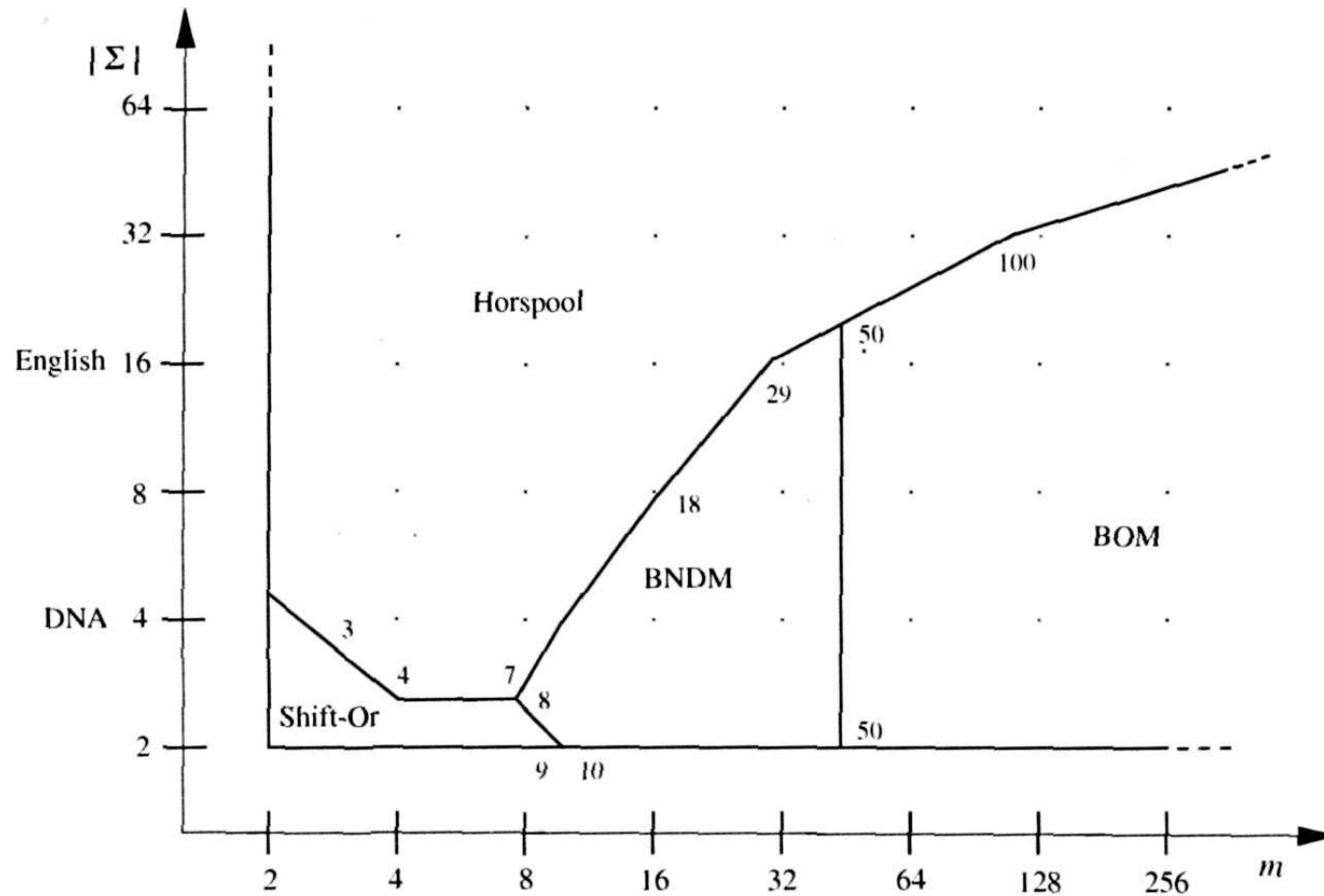
Overview of string matching algorithms

Algorithm	Worst case	Average case	Comp.	Note
Trivial	$O(nm)$	$O(n + m)$	Y	simple
DFA	$O(n + \sigma m)$	$O(n + \sigma m)$	N	real-time
(K)MP	$O(n + m)$	$O(n + m)$	Y	
Boyer Moore	$O(nm), O(n + m)$	$O(\frac{n}{\sigma} + m)$	N	
Rabin-Karp	$O(nm)$	$O(n + mk)$	N	randomized
Shift-and	$O(n + m + \sigma)$	$O(n + m + \sigma)$	N	m-bit register
BNDM	$O(nm + \sigma)$	$O(n^{\frac{\log_{\sigma} m}{m}} + m + \sigma)$	N	m-bit register

Multiple patterns: Aho Corasick $O((n + m) \log \sigma + k)$

2D patterns: Baker Bird $O((n + m) \log \sigma)$

Fastest algorithm for various m and σ



Navarro, Raffinot (2002) Flexible Pattern Matching in Strings.

Random texts, 32-bit numbers

Nepovinná domáca úloha

V Boyer-Moorovom algoritme s použitím iba slabého pravidla dobrého sufixu nájdite príklady P a T , ktoré vyžadujú kvadratický počet porovnaní, aj keď sa P v T nenachádza.

Boyerov-Moorov algoritmus 1977

```
1  i = 0;
2  while ( i <= n - m ) {
3      j = m - 1;
4      while ( j >= 0 && P[j] == T[i + j] ) {
5          j —;
6      }
7      if ( j < 0 ) { print i; }
8      i += skip;
9  }
```

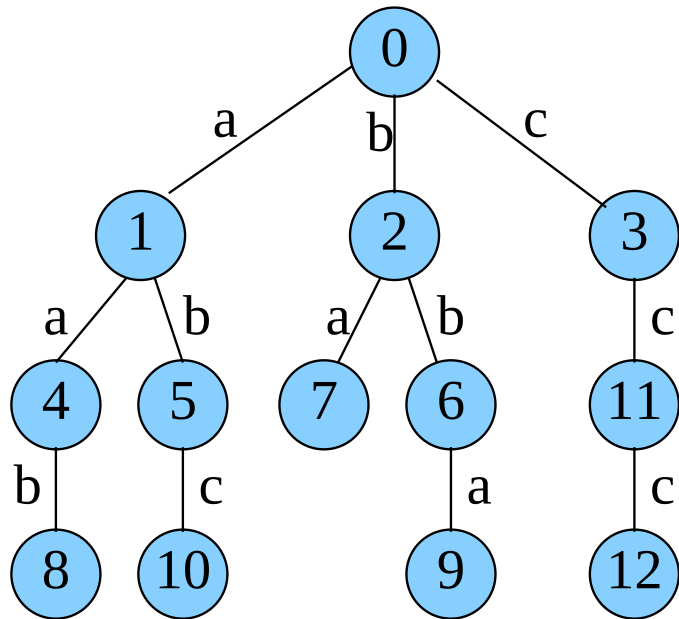
Good suffix rule: skip $\gamma[j]$:

$$\gamma[j] = m - \max\{k \mid 0 \leq k < m \wedge P[j + 1..m - 1] \sim P[0..k - 1]\}$$

$P \sim Q$ iff P is a suffix of Q or Q is a suffix of P

LZW compression (Lempel–Ziv–Welch 1984)

Used in GIF, popular UNIX compression in the past, formerly patent issues



Original text: aabbaabbabcccccc

Compressed: 1, 1, 2, 2, 4, 6, 5, 3, 11, 12